So You Think You're Fast: Performance Evaluation of Two High-Performance Software Libraries

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Outline

► schnaps

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- A discontinuous Galerkin solver in OpenCL
- How can we evaluate it's performance?
 - Roofline
 - Profiling
 - Benchmarking
- ► fftw++
 - ► A wrapper for FFTW
 - Implicitly dealiased convolutions
 - How can we compare two different algorithms?

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Solveur pour les lois de Conservation Hyperboliques Non-linéaires Appliqué aux PlasmaS

Solver for Conservative Hyperbolic Non-linear systems for PlasmaS

- Discontinuous Galerkin solver for hyperbolic equations
- ▶ Written in OpenCL for GPUs, CPUs, etc.
- > gforge.inria.fr/projects/schnaps

Collaborators: Philippe Helluy, Emmanuel Franck, Michel Massaro, Bruno Weber, ...

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Consider the general hyperbolic equation

$$\partial_t w + \sum_{k=1}^{k=d} \partial_k F^k(w) = S,$$
 (1)

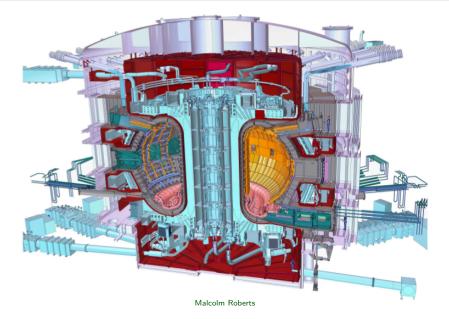
in d = dimensions. F is the flux and S the source term.

Examples:

- Navier–Stokes equations
- Maxwell's equations
- MHD
- Vlasov equations

We would like to numerically solve such equations in complex geometries with as general boundary conditions as possible.

schnaps example: Vlasov equations for fusion



schnaps: Discontinuous Galerkin Method

The physical domain is divided into cells. In each cell *L*, *w* is projected onto a finite set of basis functions $\psi_i^L(x)$:

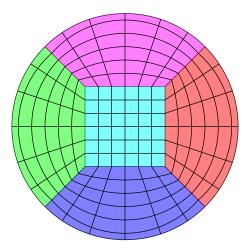
$$w(x,t) \approx \sum_{i \in L} w_L^i(t) \psi_i^L(x).$$
(2)

The evolution equation is approximated by

$$\int_{L} \partial_{t} w \psi_{i}^{L} - \int_{L} F(w, w, \nabla \psi_{i}^{L}) + \int_{\partial L} F(w_{L}, w_{R}, \boldsymbol{n}_{LR}) \psi_{i}^{L} = S_{i}^{L},$$
(3)

where n_{LR} is the normal vector from cell *L* to cell *R*. The DG formulation is good for conserving invariants. Elements can be curved and meshes can be non-conformal.

schnaps: Macrocell/subcell



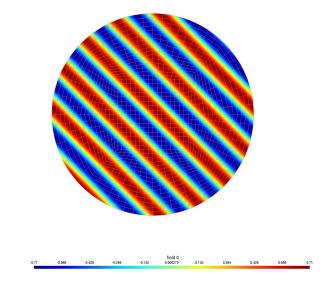
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There computational stages are:

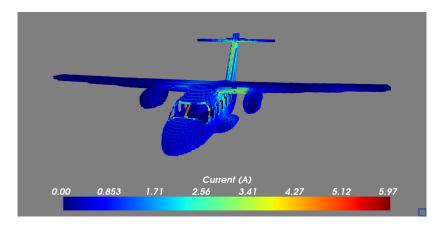
- 1. Initialize the buffer.
- 2. Compute boundary flux.
- 3. Compute macrocell interface flux.
- 4. Compute subcell interfaces flux.
- 5. Compute volumic flux.
- 6. Compute source term.
- 7. Apply the mass division.
- 8. Time-step.

schnaps example simulation: Maxwell's equations



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schnaps example simulation: Maxwell's equations

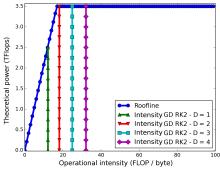


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schnaps: roofline analysis

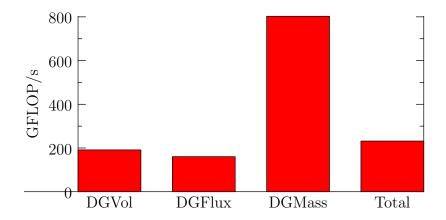
Roofline: Count FLOPs, count i/o, compare with manufacturer specs.

- ► Compare the achieved vs theoretical FLOPs and i/o.
- ► Manufacturer specifications are available for most GPUs.



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schnaps: roofline analysis



schnaps: profiling

OpenCL provides profiling tools.

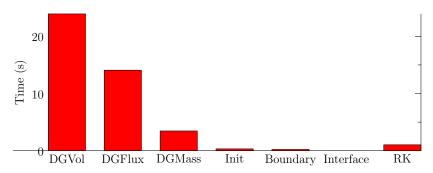
- We can find the start and end times for a kernel
- Reports ns time (accurate to \approx 50ns).

Profiling is complicated in an OpenCL environment:

- Kernel execution might be overlapped
- Kernels are launched into a queue, and we need to wait until it's done before asking for the execution time.

schnaps: profiling

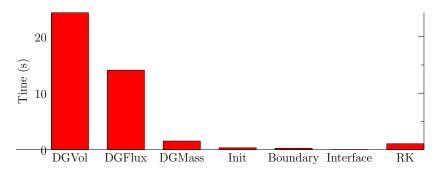
Total execution times for all kernels:



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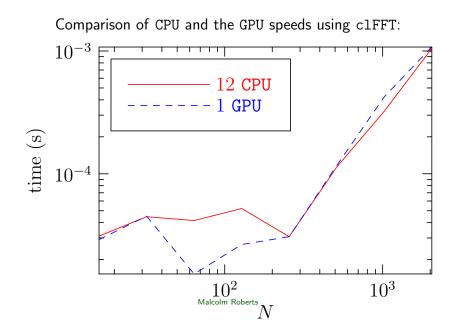
schnaps: profiling

Total execution times with mass pre-computed:

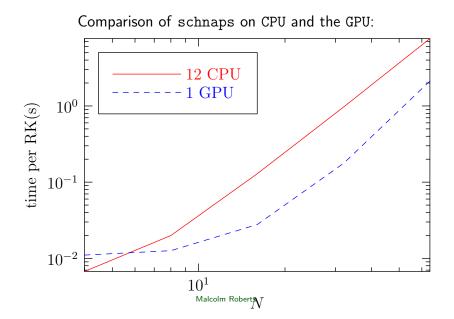


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schnaps: benchmarking the CPU and the GPU



schnaps: benchmarking the CPU and the GPU



schnaps: other geometries

The timing examples were for a mesh with one macrocell. The macrocell interfaces are complicated:

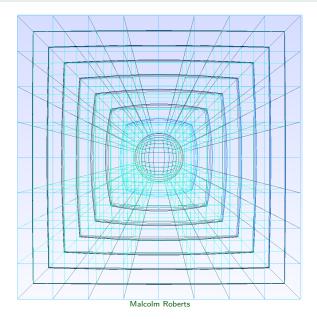
- Non-coalescent memory access
- Changes of geometry
- ► Parallel computation not straightforward.

Two options for parallelizing macrocell interfaces:

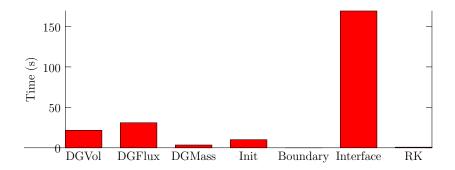
- ► In-place, use map-colouring for parallelism
- Extraction, computation in parallel, insertion.

Also reducing computational complexity.

schnaps: other geometries



schnaps: other geometries



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schnaps: summary

- ► Roofline predicts how fast your code will be.
- Profiling tells you where you need to work.
- Benchmarking tells you your speed.
- Intra-macrocell code looks ok.
- Inter-macrocell code needs work.

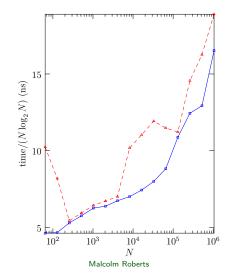
fftw++ offers:

- ► C++ wrappers for FFTW
- Implementations of implicitly dealiased convolutions.
- New MPI routines in 2.0:
 - Adaptive recursive non-blocking transpose
 - MPI version of convolutions and FFTs
 - 2D data decomposition
- fftwpp.sf.net.

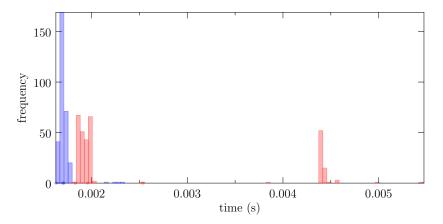
Collaborator: John Bowman.

We need to test the speed of these routines.

Timing 1D convolution on Atlas:

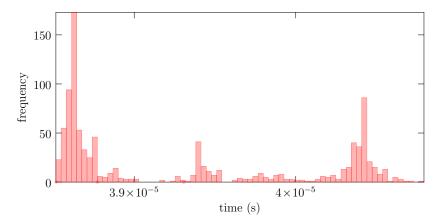


Histogram of execution times on Atlas:



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Histogram of cIFFT execution times on a K40:

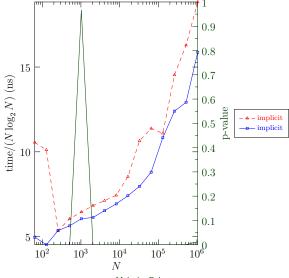


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We need stats!

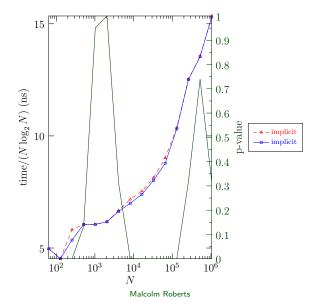
- The mean is not a good measure.
- ► We can't predict the confidence for the minimum.
- ► So, we should look at the median time.
- ► We need statistical tests; look at Mood's Median test.
 - Or the Wilcoxon signed-rank test, etc.
- Applications: publishing papers, self-tuning software libraries.

fftw++: sequential tests

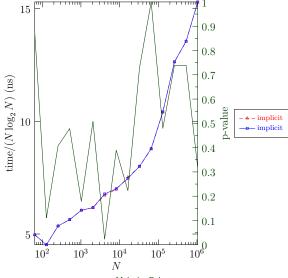


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fftw++: alternating tests

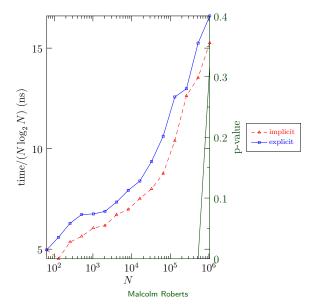


fftw++: randomizing tests

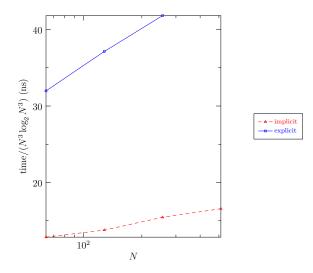


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fftw++: randomizing tests, different algorithms



fftw++: Comparison of 3D routine



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fftw++: conclusion

- Noise can have a large affect on timing algorithms!
- Running algorithms in series gives noisy results.
- ► Randomizing the algorithm order gives the best results.
- We can (and probably should) use some stats.

Conclusion

I presented the analysis of two software packages. schnaps:

- ► Looked at: roofline, profiling, and benchmarks.
- ► It's fast, but comparison is difficult.
- ► The macrocell interfaces will be faster soon.

fftw++:

- ► We found a way to deal with noise when timing.
- ► Now we re-write a bunch of scripts. :(
- But the results look good so far!

Thank you for your attention! Merci pour votre attention!