

A.2 Table of Laplace Transforms

$f(t)$	$\mathcal{L}(f) = F(s)$
$f'(t)$	$sF(s) - f(0)$
$f''(t)$	$s^2F(s) - sf(0) - f'(0)$
$f^{(n)}(t)$	$s^nF(s) - s^{n-1}f(0) - \dots - f^{(n-1)}(0)$
t^n	$\frac{n!}{s^{n+1}}$
$e^{\alpha t}$	$\frac{1}{s - \alpha}$
$e^{\alpha t}f(t)$	$F(s - \alpha)$
$f(ct)$	$\frac{1}{c}F\left(\frac{s}{c}\right)$
$\cos(\beta t)$	$\frac{s}{s^2 + \beta^2}$
$\sin(\beta t)$	$\frac{\beta}{s^2 + \beta^2}$
$\cosh(\beta t)$	$\frac{s}{s^2 - \beta^2}$
$\sinh(\beta t)$	$\frac{\beta}{s^2 - \beta^2}$
$e^{\alpha t} \cos(\beta t)$	$\frac{s - \alpha}{(s - \alpha)^2 + \beta^2}$
$e^{\alpha t} \sin(\beta t)$	$\frac{\beta}{(s - \alpha)^2 + \beta^2}$
$u_c(t), c > 0$	e^{-cs}/s
$u_c(t)f(t - c), c > 0$	$e^{-cs}F(s)$
$\delta(t - c), c > 0$	e^{-cs}
$\int_0^t f(t - \tau)g(\tau) d\tau \doteq f * g$	$F(s)G(s)$
$f(t)$ with $f(t + T) = f(t)$	$\frac{\int_0^T f(t)e^{-st} dt}{1 - e^{-sT}}$
$t^n f(t)$	$(-1)^n \frac{d^n}{ds^n} F(s)$